Make this Foldable to help you organize information about the material in this chapter. Begin with three sheets of plain $8\frac{1}{2}$ by 11" paper.

1. **Fold** in half along the width.

2. **Open** and fold the bottom to form a pocket. Glue edges.

3. **Repeat** steps 1 and 2 three times and glue all three pieces together.

4. **Label** each pocket with the lesson names. Place an index card in each pocket.

**Reading and Writing** As you read and study the chapter, you can write the main ideas, examples of theorems, and postulates on the index cards.
Problem-Solving Workshop

Project

Your school newspaper is holding a photography contest. The theme is parallel lines. To enter, you must submit a portfolio containing five photographs, or copies of photographs, of parallel lines in the real world. How can you create a portfolio that has a good chance of winning?

Working on the Project

Work with a partner and choose a strategy to complete this project. Here are some suggestions.

- Define parallel lines.
- Research how newspapers use parallel lines.
- Discuss where you might find parallel lines in the real world. Compile a list.
- Decide what photographs you want to use.

Technology Tools

- Use a scanner and scanning software to enhance your photographs.
- Use word processing software to write a caption describing each photograph and to answer the questions below.

Research

For more information about photojournalism, visit: www.geomconcepts.com

Presenting the Project

Your portfolio should contain five original photographs or copies. Each photograph along with its caption should be on a separate page. Each page should also contain answers to the following questions.

- What is the object in the photograph?
- Where are the parallel lines and how can you justify that they are parallel?
- Is there a transversal shown in the photograph? If so, describe the object that is acting as a transversal.
- What real-life problems would arise if the lines in this object were not parallel?
Suppose you could measure the distance between the columns of a building at various points. You would find that the distance remains the same at all points. The columns are parallel.

In geometry, two lines in a plane that are always the same distance apart are parallel lines. No two parallel lines intersect, no matter how far you extend them.

Since segments and rays are parts of lines, they are considered parallel if the lines that contain them are parallel.

Planes can also be parallel. The shelves in a bookcase are examples of parts of planes. The shelves are the same distance apart at all points, and do not appear to intersect. They are parallel. In geometry, planes that do not intersect are called parallel planes.
Sometimes lines that do not intersect are not in the same plane. These lines are called **skew lines**.

**Definition of Skew Lines**

Two lines that are not in the same plane are skew if and only if they do not intersect.

Segments and rays can also be skew if they are contained in skew lines. In the figure, \( AX \) and \( BC \) are skew segments. They are parts of noncoplanar lines that do not intersect. \( AX \) and \( XZ \) intersect at \( X \). They are not skew segments.

**Examples**

Name the parts of the rectangular prism shown below. Assume segments that look parallel are parallel.

1. all planes parallel to plane \( ABC \)
   
   Plane \( ABC \) is parallel to plane \( EFG \).

2. all segments that intersect \( AB \)
   
   \( BC, AD, AH, AE, \) and \( BF \) intersect \( AB \).

3. all segments parallel to \( FG \)
   
   \( BC, AD, \) and \( EH \) are parallel to \( FG \).

4. all segments skew to \( EF \)
   
   \( CG, DH, AD, BC, \) and \( AH \) are skew to \( EF \).

**Your Turn**

Name the parts of the figure above.

a. all planes parallel to plane \( ABF \)

b. all segments that intersect \( DH \)

c. all segments parallel to \( CD \)

d. all segments skew to \( AB \)
1. **Draw and label** two parallel lines, \( \ell \) and \( m \). Indicate that the lines are parallel by using the arrowhead symbol.

2. **Describe** a real-world example or model of parallel lines.

3. **Sketch** the diagram shown below in your journal. Then describe and explain the relationship between lines \( \ell \) and \( m \).

   ![Diagram of parallel lines]

   **Planes A and B are parallel.**

**Guided Practice**

Describe each pair of segments in the prism as **parallel**, **skew**, or **intersecting**.  
*(Examples 2–4)*

4. \( KN, HL \)
5. \( JM, ML \)
6. \( JM, KH \)

**Name the parts of the cube shown at the right.** *(Examples 1, 3, & 4)*

7. all planes parallel to plane \( WXQ \)
8. all segments parallel to \( PQ \)
9. all segments skew to \( PS \)
10. all pairs of parallel planes

11. **Carpentry** A carpenter is constructing a chair like the one shown at the left. Describe a pair of parts that are parallel, a pair that intersect, and a pair that are skew. *(Examples 2–4)*
Describe each pair of segments in the prism as parallel, skew, or intersecting.

12. \(BE, CF\)  
13. \(AD, BE\)  
14. \(AD, EF\)  
15. \(BC, EF\)  
16. \(AB, DE\)  
17. \(AB, CF\)  
18. \(AB, BC\)  
19. \(AD, BC\)  
20. \(BE, BC\)  
21. \(BC, DE\)

Name the parts of the cube shown at the right.

22. six planes  
23. all pairs of parallel planes  
24. all segments parallel to \(EH\)  
25. all segments skew to \(GH\)  
26. all segments parallel to \(AE\)  
27. all segments skew to \(BF\)

Name the parts of the pyramid shown at the right.

28. all pairs of intersecting planes  
29. all pairs of parallel segments  
30. all pairs of skew segments  
31. all sets of three segments that intersect in a common point

Draw and label a figure to illustrate each pair.

32. congruent parallel segments  
33. parallel segments not congruent  
34. segments not parallel or congruent  
35. skew segments  
36. segments not intersecting or skew  
37. parallel planes  
38. intersecting planes  
39. parallel rays
Complete each sentence with *sometimes*, *always*, or *never*.

40. Skew lines ___?___ intersect.
41. Skew lines are ___?___ parallel.
42. Two parallel lines ___?___ lie in the same plane.
43. Two lines in parallel planes are ___?___ skew.
44. Two lines that have no points in common are ___?___ parallel.
45. If two lines are parallel, then they ___?___ lie in the same plane.

46. **Interior Design** The shower stall shown in the diagram is formed by a series of intersecting planes. Name two skew segments in the diagram.

47. **Construction** The Empire State Building, built in 1930–1931, is 102 stories and reaches a height of 1250 feet. Suppose the stories represent parallel planes equal distances apart. What is the approximate distance between floors?

48. **Sports** Describe how skis on a skier’s feet could *intersect*, be *parallel*, or be *skew*.

49. **Graphic Arts** The comic artist has used parallel lines two ways in the *B.C.* comic below. Explain the two uses of parallel lines in the comic.
50. **Critical Thinking**  Plane $A$ is parallel to plane $B$, and plane $B$ is parallel to plane $C$. Is Plane $A$ parallel to Plane $C$? Write yes or no, and explain your answer. Then describe something in your school building that illustrates your response.

Mixed Review

51. In the figure at the right, $BE \perp AD$.  
   a. Name four right angles.
   b. Name a pair of supplementary angles.
   c. Name two pairs of angles whose sum is 90.

52. If $\angle JKL \cong \angle PQR$, $m\angle PQR = 4x + 5$, and $m\angle JKL = 5x - 12$, what is $m\angle PQR$?  
   (Lesson 3–6)

Refer to the figure at the right.  
(Lesson 3–3)

53. If $m\angle CAE = 78$ and $m\angle DAE = 30$, find $m\angle 1$.

54. Find $m\angle DAF$ if $m\angle DAE = 30$ and $m\angle EAF = 75$.

55. **Time**  Do the hands of a clock at 12:20 P.M. form an acute, obtuse, or right angle?  
   (Lesson 3–2)

56. **Cartography**  On a map of Ohio, Cincinnati is located at (3, 5), and Massillon is located at (17, 19). If Columbus is halfway between the two cities, what ordered pair describes its position?  
   (Lesson 2–5)

57. It is 4.5 blocks from Carlos’ house to Matt’s house. From Matt’s house to Keisha’s house is 10.5 blocks, and from Keisha’s house to Carlos’ house is 6 blocks. If they live on the same street, whose house is between the other two?  
   (Lesson 2–2)

58. **Short Response**  Name all the planes that can contain three of the points $J$, $K$, $L$, and $M$, if no three points are collinear and the points do not all lie in the same plane.  
   (Lesson 1–3)

59. **Multiple Choice**  12 is what percent of 40?  
   A $0.3\%$  
   B $3\frac{1}{3}\%$  
   C $30\%$  
   D $33\%$  
   (Percent Review)

www.geomconcepts.com/self_check_quiz
In geometry, a line, line segment, or ray that intersects two or more lines at different points is called a **transversal**. \( \overline{AB} \) is an example of a transversal. It intersects lines \( \ell \) and \( m \). Note all of the different angles that are formed at the points of intersection.

When a transversal intersects two lines, eight angles are formed, as shown in the figures above. These angles are given special names.

- **Interior angles** lie between the two lines. 
  \( \angle 3, \angle 4, \angle 5, \angle 6 \)
- **Alternate interior angles** are on opposite sides of the transversal. 
  \( \angle 3 \) and \( \angle 5 \), \( \angle 4 \) and \( \angle 6 \)
- **Consecutive interior angles** are on the same side of the transversal. 
  \( \angle 3 \) and \( \angle 6 \), \( \angle 4 \) and \( \angle 5 \)

- **Exterior angles** lie outside the two lines. 
  \( \angle 1, \angle 2, \angle 7, \angle 8 \)
- **Alternate exterior angles** are on opposite sides of the transversal. 
  \( \angle 1 \) and \( \angle 7 \), \( \angle 2 \) and \( \angle 8 \)
Identify each pair of angles as alternate interior, alternate exterior, consecutive interior, or vertical.

1. ∠2 and ∠8
   ∠2 and ∠8 are exterior angles on opposite sides of the transversal, so they are alternate exterior angles.

2. ∠1 and ∠6
   ∠1 and ∠6 are interior angles on the same side of the transversal, so they are consecutive interior angles.

Your Turn

a. ∠2 and ∠4  

b. ∠4 and ∠6

In the following activity, you will investigate the relationships among the angles formed when a transversal intersects two parallel lines.

Materials:
- lined paper
- straightedge
- protractor

Step 1 Use a straightedge to darken any two horizontal lines on a piece of lined paper.

Step 2 Draw a transversal for the lines and label the angles 1 through 8. Use a protractor to find the measure of each angle.

Try These
1. Compare the measures of the alternate interior angles.
2. What is the sum of the measures of the consecutive interior angles?
3. Repeat Steps 1 and 2 above two more times by darkening different pairs of horizontal lines on your paper. Make the transversals intersect the lines at a different angle each time.
4. Do the interior angles relate to each other the same way for each pair of lines?
5. Compare the measures of the alternate exterior angles in each drawing.
The results of the activity suggest the theorems stated below.

<table>
<thead>
<tr>
<th>Theorem</th>
<th>Words</th>
<th>Models and Symbols</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>4–1</strong></td>
<td><strong>Alternate Interior Angles</strong> If two parallel lines are cut by a transversal, then each pair of alternate interior angles is congruent.</td>
<td>![Diagram of Alternate Interior Angles]</td>
</tr>
<tr>
<td><strong>4–2</strong></td>
<td><strong>Consecutive Interior Angles</strong> If two parallel lines are cut by a transversal, then each pair of consecutive interior angles is supplementary.</td>
<td>![Diagram of Consecutive Interior Angles]</td>
</tr>
<tr>
<td><strong>4–3</strong></td>
<td><strong>Alternate Exterior Angles</strong> If two parallel lines are cut by a transversal, then each pair of alternate exterior angles is congruent.</td>
<td>![Diagram of Alternate Exterior Angles]</td>
</tr>
</tbody>
</table>

You can use these theorems to find the measures of angles.

**Examples**

3. In the figure, \( p \parallel q \), and \( r \) is a transversal. If \( m\angle 5 = 28 \), find \( m\angle 8 \).

\( \angle 5 \) and \( \angle 8 \) are alternate exterior angles, so by Theorem 4–3 they are congruent. Therefore, \( m\angle 8 = 28 \).

4. In the figure, \( \overline{AB} \parallel \overline{CD} \), and \( t \) is a transversal. If \( m\angle 8 = 68 \), find \( m\angle 6, m\angle 7, \) and \( m\angle 9 \).

\( \angle 6 \) and \( \angle 8 \) are consecutive interior angles, so by Theorem 4–2 they are supplementary.

\[
\begin{align*}
m\angle 6 + m\angle 8 &= 180 \\
m\angle 6 + 68 &= 180 \\
m\angle 6 &= 112
\end{align*}
\]

Replace \( m\angle 8 \) with 68.

Subtract 68 from each side.

\[
\begin{align*}
m\angle 6 &= 112
\end{align*}
\]

\( \angle 7 \) and \( \angle 8 \) are alternate interior angles, so by Theorem 4–1 they are congruent. Therefore, \( m\angle 7 = 68 \).
\[ \angle 6 \text{ and } \angle 9 \text{ are alternate interior angles, so by Theorem 4–1 they are congruent. Thus, } m\angle 9 = 112. \]

**Look Back**

Linear Pairs: Lesson 3–4; Supplement Postulate: Lesson 3–5

**Example**

5

**Algebra Link**

- Solving Equations with the Variable on Both Sides, p. 724

**Your Turn**

Refer to the figure in Example 3. Find the measure of each angle.

c. \( \angle 1 \)
d. \( \angle 2 \)
e. \( \angle 3 \)
f. \( \angle 4 \)

g. Find \( m\angle GCH \).

In the figure, \( s \parallel t \), and \( m \) is a transversal. Find \( m\angle EBF \).

By Theorem 4–1, \( \angle ABC \) is congruent to \( \angle BCD \).

\[
\begin{align*}
m\angle ABC &= m\angle BCD & \text{Congruent angles have equal measures.} \\
3x - 5 &= 4x - 29 & \text{Substitution} \\
3x - 5 - 3x &= 4x - 29 - 3x \\
-5 &= x - 29 \\
-5 + 29 &= x - 29 + 29 & \text{Add 29 to each side.} \\
24 &= x
\end{align*}
\]

The measure of \( \angle ABC \) is \( 3x - 5 \).

\[
\begin{align*}
m\angle ABC &= 3x - 5 \\
m\angle ABC &= 3(24) - 5 & \text{Replace } x \text{ with 24.} \\
&= 72 - 5 & \text{or 67}
\end{align*}
\]

\( \angle EBF \) and \( \angle ABC \) are vertical angles and are therefore congruent.

\[
m\angle EBF = m\angle ABC & \quad \text{Congruent angles have equal measures.} \\
&= 67 & \text{Substitution}
\]

**Your Turn**

\( g. \) Find \( m\angle GCH \).

**Check for Understanding**

**Communicating Mathematics**

1. **Explain** why \( \angle 2 \) and \( \angle 3 \) must be congruent.

2. **Describe** two different methods you could use to find \( m\angle 3 \) if \( m\angle 1 = 130 \).

**Vocabulary**

transversal
interior angles
alternate interior angles
consecutive interior angles
exterior angles
alternate exterior angles

Lesson 4–2 Parallel Lines and Transversals 151
3. Name each transversal and the lines it intersects in the figure at the right.

Guided Practice

Identify each pair of angles as alternate interior, alternate exterior, consecutive interior, or vertical. (Examples 1 & 2)

4. \( \angle 3 \) and \( \angle 7 \)
5. \( \angle 1 \) and \( \angle 5 \)
6. \( \angle 2 \) and \( \angle 8 \)
7. \( \angle 2 \) and \( \angle 3 \)

\( a \parallel b \), and \( h \) is a transversal. If \( \angle 1 = 48 \), find the measure of each angle. Give a reason for each answer. (Examples 3 & 4)

8. \( \angle 2 \)
9. \( \angle 3 \)
10. \( \angle 4 \)
11. \( \angle 7 \)

12. Algebra In the figure at the right, \( r \parallel t \), and \( d \) is a transversal. Find \( \angle 1 \) and \( \angle 2 \). (Example 5)

Exercises

Practice

Identify each pair of angles as alternate interior, alternate exterior, consecutive interior, or vertical.

13. \( \angle 1 \) and \( \angle 5 \)
14. \( \angle 2 \) and \( \angle 10 \)
15. \( \angle 5 \) and \( \angle 15 \)
16. \( \angle 11 \) and \( \angle 3 \)
17. \( \angle 1 \) and \( \angle 4 \)
18. \( \angle 16 \) and \( \angle 8 \)
19. \( \angle 5 \) and \( \angle 6 \)
20. \( \angle 10 \) and \( \angle 14 \)
21. \( \angle 15 \) and \( \angle 14 \)
22. \( \angle 8 \) and \( \angle 2 \)
23. \( \angle 12 \) and \( \angle 14 \)
24. \( \angle 9 \) and \( \angle 13 \)

Find the measure of each angle. Give a reason for each answer.

25. \( \angle 1 \)
26. \( \angle 4 \)
27. \( \angle 6 \)
28. \( \angle 5 \)
Find the measure of each angle. Give a reason for each answer.

29. \( \angle 9 \)  
30. \( \angle 12 \)  
31. \( \angle 13 \)  
32. \( \angle 15 \)  
33. \( \angle 19 \)  
34. \( \angle 21 \)  
35. \( \angle 22 \)  
36. \( \angle 24 \)  

Find the values of \( x \) and \( y \).

37.  

38.  

39.  

Road Maps  Trace and label a section of a road map that illustrates two parallel roads intersected by a transversal road or railroad. Use a protractor to measure the angles formed by the intersections on the map. How does this drawing support Theorems 4–1, 4–2, and 4–3?

Construction  The roof at the right intersects the parallel lines of the siding. Which angles are congruent?

Critical Thinking  In the figure at the right, explain why you can conclude that \( \angle 1 \equiv \angle 4 \), but you cannot tell whether \( \angle 3 \) is congruent to \( \angle 2 \).

Mixed Review  

Draw and label a cube. Name the following pairs.  

43. parallel segments  
44. intersecting segments  
45. skew segments  

46. In the figure at the right, \( \overline{AD} \perp \overline{CD} \). If \( m \angle ADB = 23 \) and \( m \angle BDC = 3y - 2 \), find \( y \).  

Draw and label a coordinate plane on a piece of grid paper. Then graph and label each point.  

47. \( G(-5, -1) \)  
48. \( H(3, -2) \)  
49. \( J(4, 0) \)  

50. Short Response  Write a sequence of five numbers that follows the pattern +1, +3, +5, . . . .
Investigation

When Does a Circle Become a Line?

Materials
- globe
- two large rubber bands
- removable tape
- ruler
- protractor
- scissors

Spherical Geometry

The geometry you have been studying in this text is called Euclidean geometry. It was named for a famous Greek mathematician named Euclid (325 B.C.–265 B.C.). There are, however, other types of geometry. Let’s take a look at spherical geometry. Spherical geometry is one form of non-Euclidean geometry.

Investigate

1. Use a globe, two large rubber bands, and the steps below to investigate lines on a sphere.

   a. In Euclidean and spherical geometry, points are the same. A point is just a location that can be represented by a dot.

   b. In Euclidean geometry, you can represent a plane by a sheet of paper. Remember that the paper is only part of the plane. The plane goes on forever in all directions. In spherical geometry, a plane is a sphere. The sphere is finite, that is, it does not go on forever. The globe will represent a plane in spherical geometry for this investigation.

   c. If possible, place a large rubber band on the globe covering the equator. The equator is known as a line in spherical geometry. In Euclidean geometry, a line extends without end in both directions. In spherical geometry, a line is finite. In spherical geometry, a line is defined as a great circle, which divides a sphere into two congruent halves. On the globe, the equator is also called a line of latitude.

   d. Place a second large rubber band on the globe so that it extends over both the North and South Poles. Position the band so that it is also a great circle. On the globe, a line like this is also called a line of longitude.

   e. In Euclidean geometry you learned that when two lines intersect, they have only one point in common. Look at the rubber bands on your globe. How many points do these two lines have in common?
2. Use the globe, removable tape, and the steps below to investigate angle measures in spherical and Euclidean planes.
   
a. Select two points on the equator. Select another point close to the North Pole. Use three pieces of removable tape to form a triangle as shown. Use a protractor to estimate the measure of each angle of the triangle. Record your results.

b. Carefully remove the tape from the sphere. Use the three strips to form a triangle on a sheet of paper. Use a protractor to estimate the measure of each angle of the triangle. Record the results.

c. You have formed two triangles with sides of the same length. The first was on the spherical plane. The second was on the Euclidean plane. How do the angle measures of the two triangles compare?

In this extension, you will investigate lines in both Euclidean and spherical geometry by using a globe or geometry drawing software.

1. Determine whether all lines of longitude on the globe are lines in spherical geometry.

2. Determine whether all lines of latitude on the globe are lines in spherical geometry.

3. In Chapter 3, you learned the theorem that states: if two lines are perpendicular, then they form four right angles. Is this theorem true for spherical geometry? Explain your reasoning and include a sketch.

4. Make a conjecture about angle measures of triangles in Euclidean and spherical geometry. Use at least three different-sized triangles to support your idea.

Presenting Your Conclusions

Here are some ideas to help you present your conclusions to the class.

- Make a poster comparing a point, a line, and a plane in Euclidean geometry and spherical geometry. Include diagrams or sketches.
- Research parallel lines in spherical geometry. Write a paragraph to report your findings.
- Make a video demonstrating your findings in the project.
- Pair up with another group. Have a debate in which one group is in favor of Euclidean geometry, and the other is in favor of spherical geometry.

For more information on non-Euclidean geometry, visit: www.geomconcepts.com
When a transversal crosses two lines, the intersection creates a number of angles that are related to each other. Note \( \angle 7 \) and \( \angle 8 \) below. Although one is an exterior angle and the other is an interior angle, both lie on the same side of the transversal.

Angles 7 and 8 are called **corresponding angles**. They have different vertices. In the figure, three other pairs of corresponding angles are formed.

Lines \( p \) and \( r \) are cut by transversal \( t \). Name two pairs of corresponding angles.

\( \angle 1 \) and \( \angle 5 \)
\( \angle 4 \) and \( \angle 7 \)

Refer to the figure above.

**a.** Name two other pairs of corresponding angles.

As with interior and exterior angles, there is a special relationship between corresponding angles when the transversal intersects parallel lines.

Recall that in Lesson 4–2, you discovered that if parallel lines are cut by a transversal, then each pair of alternate interior angles is congruent, and that each pair of consecutive interior angles is supplementary. Using the drawings you made for the Hands-On Geometry activity on page 149, measure the corresponding angles. What do you notice?
In the figure, \( \ell \parallel m \), and \( a \) is a transversal. Which angles are congruent to \( \angle 1 \)? Explain your answers.

\[
\angle 1 \cong \angle 7 \quad \text{Vertical angles are congruent.}
\]

\[
\angle 1 \cong \angle 9 \quad \text{Postulate 4–1}
\]

\[
\angle 7 \cong \angle 15 \quad \text{Postulate 4–1}
\]

Therefore, \( \angle 1 \cong \angle 7 \cong \angle 9 \cong \angle 15 \).

Find the measure of \( \angle 10 \) if \( m\angle 1 = 62 \).

\[
m\angle 1 = m\angle 9, \text{ so } m\angle 9 = 62.
\]

\[
\angle 9 \text{ and } \angle 10 \text{ are a linear pair, so they are supplementary.}
\]

\[
m\angle 9 + m\angle 10 = 180
\]

\[
62 + m\angle 10 = 180 \quad \text{Replace } m\angle 9 \text{ with } 62.
\]

\[
62 + m\angle 10 - 62 = 180 - 62 \quad \text{Subtract 62 from each side.}
\]

\[
m\angle 10 = 118
\]

**Your Turn**

In the figure above, assume that \( b \) is also a transversal.

b. Which angles are congruent to \( \angle 1 \)?

c. Find the measure of \( \angle 5 \) if \( m\angle 14 = 98 \).

Thus far, you have learned about the relationships among several kinds of special angles.

<table>
<thead>
<tr>
<th>Concept Summary</th>
<th>Types of angle pairs formed when a transversal cuts two parallel lines.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Congruent \hspace{1cm} \hspace{1cm} alternate interior \hspace{1cm} alternate exterior \hspace{1cm} corresponding</td>
</tr>
<tr>
<td></td>
<td>Supplementary \hspace{1cm} \hspace{1cm} consecutive interior</td>
</tr>
</tbody>
</table>

You can use corresponding angles to prove the relationship of a perpendicular transversal to two parallel lines. In the figure, \( r \parallel s \) and transversal \( c \) is perpendicular to \( r \).

\[
\angle 1 \text{ is a right angle.} \quad \text{Definition of perpendicular lines}
\]

\[
m\angle 1 = 90 \quad \text{Definition of right angle}
\]

\[
\angle 1 \cong \angle 2 \quad \text{Postulate 4–1}
\]

\[
m\angle 1 = m\angle 2 \quad \text{Definition of congruent angles}
\]

\[
90 = m\angle 2 \quad \text{Substitution}
\]

\[
\angle 2 \text{ is a right angle.} \quad \text{Definition of right angle}
\]

\[
c \perp s \quad \text{Definition of perpendicular lines}
\]
This relationship leads to the following theorem.

**Theorem 4–4 Perpendicular Transversal**

If a transversal is perpendicular to one of two parallel lines, it is perpendicular to the other.

In the figure, \( p \parallel q \), and transversal \( r \) is perpendicular to \( q \).

If \( m \angle 2 = 3x - 6 \), find \( x \).

\[
p \perp r \quad \text{Theorem 4–4} \\
\angle 2 \text{ is a right angle.} \\
m \angle 2 = 90 \quad \text{Definition of right angles} \\
m \angle 2 = 3x - 6 \quad \text{Given} \\
90 = 3x - 6 \quad \text{Replace } m \angle 2 \text{ with } 90. \\
90 + 6 = 3x - 6 + 6 \quad \text{Add 6 to each side.} \\
96 = 3x \quad \text{Add 6 to each side.} \\
32 = \frac{3x}{3} \quad \text{Divide each side by 3.} \\
32 = x
\]

**Your Turn**

d. Refer to the figure above. Find \( x \) if \( m \angle 2 = 2(x + 4) \).

**Check for Understanding**

1a. Identify two pairs of corresponding angles.

b. Explain why \( \angle 6 \cong \angle 4 \).

2. Kristin says that \( \angle 2 \) and \( \angle 3 \) must be supplementary. Pedro disagrees. Who is correct, and why?

3. Draw a pair of parallel lines cut by a transversal so that one pair of corresponding angles has the given measure. (Use a straightedge and protractor.)

a. 35  
   b. 90  
   c. 105  
   d. 140
Guided Practice

**Getting Ready**

Find the value of \( x \).

**Sample:** \( 5x - 9 = 2x \)

**Solution:**

\[
5x - 2x = 9 \\
3x = 9 \\
x = 3
\]

4. \( 12x = 8x + 1 \)

5. \( 3x + 6 = 4x - 7 \)

6. \( x - 10 + 7x = 180 \)

In the figure, \( s \parallel t \) and \( c \parallel d \). Name all angles congruent to the given angle. Give a reason for each answer. (Example 2)

7. \( \angle 1 \)

8. \( \angle 5 \)

Find the measure of each numbered angle. (Examples 3 & 4)

9. \( \angle \)

10. \( \angle \)

11. **Farming**

   The road shown in the diagram divides a rectangular parcel of land into two parts. If \( m\angle 6 = 52 \), find \( m\angle 1 \). (Examples 2 & 3)

12. **Algebra**

   If \( m\angle 10 = 4x - 5 \) and \( m\angle 12 = 3x + 8 \), find \( x \), \( m\angle 10 \), and \( m\angle 11 \). (Example 4)

Exercises

**Practice**

In the figure, \( a \parallel b \). Name all angles congruent to the given angle. Give a reason for each answer.

13. \( \angle 2 \)

14. \( \angle 3 \)

15. \( \angle 8 \)

16. \( \angle 9 \)

17. \( \angle 12 \)

18. \( \angle 14 \)
Find the measure of each numbered angle.

19. \(26^\circ\)  20. \(26^\circ\)

21. \(120^\circ\)  22. \(52^\circ\)

23. \(32\)  24. \(15\)

25. If \(m\angle 4 = 2x + 7\) and \(m\angle 8 = 3x - 13\), find \(x\), \(m\angle 4\), and \(m\angle 8\).

26. If \(m\angle 8 = 14x - 56\) and \(m\angle 6 = 6x\), find \(x\), \(m\angle 8\), and \(m\angle 6\).

27. If \(m\angle 1 = 5x + 8\) and \(m\angle 4 = 12x + 2\), find \(x\), \(m\angle 1\), and \(m\angle 4\).

28. If \(m\angle 6 = 5x + 25\) and \(m\angle 7 = 3x - 5\), find \(x\), \(m\angle 6\), and \(m\angle 7\).

29. **Flag Design** Trace the drawing of the flag of the Bahamas. Assume segments that appear to be parallel are parallel. Make a conjecture about which angles you can conclude are congruent and explain your reasoning. Check your conjecture by measuring the angles.
30. **City Planning** In New York City, roads running parallel to the Hudson River are named avenues, and those running perpendicular to the river are named streets. What is the measure of the angle formed at the intersection of a street and an avenue?

31. **Critical Thinking** In the figure at the right, why can you conclude that \( \angle 6 \) and \( \angle 4 \) are congruent, but you cannot state that \( \angle 6 \) and \( \angle 2 \) are congruent?

32. Find the measure of \( \angle 1 \).

33. Name all pairs of parallel lines.

34. Draw and label a figure for each situation described.

35. Algebra In the figure, \( a \parallel b \) and transversal \( t \) is perpendicular to \( a \). If \( m\angle 9 = 2x + 8 \), find \( x \).

38. **Grid In** Austin practices the flute 9 minutes the first day, 10 minutes the second day, 12 minutes the third day, and 15 minutes the fourth day. If he continues this pattern, how many minutes will Austin practice the sixth day?

39. **Multiple Choice** Simplify \( \frac{4r^3}{2r^3} \).

### Mixed Review

### Standardized Test Practice

### Quiz 1

**Lesson 4–1 through 4–3**

1. Give examples of parallel lines and transversals as they are used in home design.

2. In the figure, \( m\angle 2 = 56 \). Find the measure of each angle.

3. Algebra In the figure, \( a \parallel b \) and transversal \( t \) is perpendicular to \( a \). If \( m\angle 9 = 2x + 8 \), find \( x \).
We can use geometry to prove that lines are parallel. We can also use geometry to construct parallel lines.

**Hands-On Geometry Construction**

**Materials:**  
- straightedge  
- compass

**Step 1**  
Use a straightedge to draw a line $\ell$ and a point $P$, not on $\ell$.

**Step 2**  
Draw a line $t$ through $P$ that intersects line $\ell$. Label $\angle 1$ as shown.

**Step 3**  
Use a compass and a straightedge to construct an angle congruent to $\angle 1$ at $P$. Label this angle $2$.

**Step 4**  
Extend the side of $\angle 2$ to form line $m$.

**Try These**

1. Identify the special angle pair name for $\angle 1$ and $\angle 2$.
2. Use a ruler to measure the distance between lines $\ell$ and $m$ at several places. Make a conjecture about the relationship between the lines.

This activity illustrates a postulate that helps to prove two lines are parallel. This postulate is the converse of Postulate 4–1.

**Postulate 4–2**

**Words:** In a plane, if two lines are cut by a transversal so that a pair of corresponding angles is congruent, then the lines are parallel.

**Model:**

$\angle 1 \cong \angle 2 \Rightarrow a \parallel b$.

**Symbols:**

If $\angle 1 \cong \angle 2$, then $a \parallel b$. 
You can use Postulate 4–2 to find the angle measures of corresponding angles so that two lines are parallel.

The intersection at the right is called a *trumpet interchange*. If \( m \angle 1 = 13x - 8 \) and \( m \angle 2 = 12x + 4 \), find \( x \) so that \( \ell \parallel m \).

From the figure, you know that \( \angle 1 \) and \( \angle 2 \) are corresponding angles. So, according to Postulate 4–2, if \( m \angle 1 = m \angle 2 \), then \( \ell \parallel m \).

\[
\begin{align*}
m \angle 1 &= m \angle 2 \\
13x - 8 &= 12x + 4 & \text{Substitution} \\
13x - 8 - 12x &= 12x + 4 - 12x & \text{Subtract 12x from each side.} \\
x - 8 &= 4 \\
x - 8 + 8 &= 4 + 8 & \text{Add 8 to each side.} \\
x &= 12 \\
m \angle 1 &= 13x - 8 \\
&= 13(12) - 8 \text{ or } 148 \\
m \angle 2 &= 12x + 4 \\
&= 12(12) + 4 \text{ or } 148
\end{align*}
\]

**Your Turn**

Refer to the figure in Example 1.

a. Find \( m \angle 3 \) and name the type of angle pair formed by \( \angle 2 \) and \( \angle 3 \).

b. Make a conjecture about the relationship between \( \angle 2 \) and \( \angle 3 \) that must be true for \( \ell \) to be parallel to \( m \).

Example 1 illustrates four additional methods for proving that two lines are parallel. These are stated as Theorems 4–5, 4–6, 4–7, and 4–8.

<table>
<thead>
<tr>
<th>Theorem</th>
<th>Words</th>
<th>Models and Symbols</th>
</tr>
</thead>
<tbody>
<tr>
<td>4–5</td>
<td>In a plane, if two lines are cut by a transversal so that a pair of alternate interior angles is congruent, then the two lines are parallel.</td>
<td><img src="image1" alt="Diagram" /> If ( \angle 1 \equiv \angle 2 ), then ( a \parallel b ).</td>
</tr>
<tr>
<td>4–6</td>
<td>In a plane, if two lines are cut by a transversal so that a pair of alternate exterior angles is congruent, then the two lines are parallel.</td>
<td><img src="image2" alt="Diagram" /> If ( \angle 3 \equiv \angle 4 ), then ( a \parallel b ).</td>
</tr>
</tbody>
</table>
So, we now have five ways to prove that two lines are parallel.

<table>
<thead>
<tr>
<th>Theorem</th>
<th>Words</th>
<th>Models and Symbols</th>
</tr>
</thead>
<tbody>
<tr>
<td>4–7</td>
<td>In a plane, if two lines are cut by a transversal so that a pair of consecutive interior angles is supplementary, then the two lines are parallel.</td>
<td><img src="image1" alt="Diagram" /> If ( m \angle 5 + m \angle 6 = 180 ), then ( a \parallel b ).</td>
</tr>
<tr>
<td>4–8</td>
<td>In a plane, if two lines are perpendicular to the same line, then the two lines are parallel.</td>
<td><img src="image2" alt="Diagram" /> If ( a \perp t ) and ( b \perp t ), then ( a \parallel b ).</td>
</tr>
</tbody>
</table>

### Concept Summary
- Show that a pair of corresponding angles is congruent.
- Show that a pair of alternate interior angles is congruent.
- Show that a pair of alternate exterior angles is congruent.
- Show that a pair of consecutive interior angles is supplementary.
- Show that two lines in a plane are perpendicular to a third line.

### Examples

2. **Identify the parallel segments in the letter Z.**

\( \angle ABC \) and \( \angle BCD \) are alternate interior angles.

\[
m \angle ABC = m \angle BCD \quad \text{Both angles measure } 40^\circ.
\]

\( AB \parallel CD \)  

*Theorem 4–5*

3. **Find the value of \( x \) so \( BE \parallel TS \).**

\( ES \) is a transversal for \( BE \) and \( TS \).

\( \angle BES \) and \( \angle EST \) are consecutive interior angles. If \( m \angle BES + m \angle EST = 180 \), then \( BE \parallel TS \) by Theorem 4–7.

4. **Your Turn**

- c. Identify any parallel segments in the letter F. Explain your reasoning.
**Algebra Review**

Solving Multi-Step Equations, p. 723

\[
m\angle BES + m\angle EST = 180
\]

\[
(2x + 10) + (5x + 2) = 180 \quad \text{Replace } m\angle BES \text{ with } 2x + 10
\]

\[
(2x + 5x) + (10 + 2) = 180 \quad \text{and } m\angle EST \text{ with } 5x + 2.
\]

\[
7x + 12 = 180
\]

\[
7x + 12 - 12 = 180 - 12
\]

\[
\frac{7x}{7} = \frac{168}{7}
\]

\[
x = 24
\]

Thus, if \( x = 24 \), then \( \overline{BT} \parallel \overline{ES} \).

**Your Turn**

d. Refer to the figure in Example 3. Find the value of \( x \) so \( \overline{BT} \parallel \overline{ES} \).

---

**Check for Understanding**

**Communicating Mathematics**

1. Explain why \( \overline{CA} \parallel \overline{RT} \) in the figure at the right.

2. Describe two situations in your own life in which you encounter parallel lines. How could you guarantee that the lines are parallel?

3. Write a step-by-step argument to show that Theorem 4–6 is true.

**Guided Practice**

Find \( x \) so that \( a \parallel b \).  **(Examples 1 & 3)**

4. \[
\begin{align*}
\angle a & = 84^\circ \\
\angle b & = 3x^\circ
\end{align*}
\]

5. \[
\begin{align*}
\angle a & = 10x^\circ \\
\angle b & = 5x^\circ
\end{align*}
\]

Name the pairs of parallel lines or segments.  **(Example 2)**

6. \[
\begin{align*}
\angle QRS & = 42^\circ \\
\angle RST & = 42^\circ
\end{align*}
\]

7. \[
\begin{align*}
\angle p & = 113^\circ \\
\angle q & = 67^\circ \\
\angle r & = 87^\circ \\
\angle s & = 68^\circ
\end{align*}
\]
Exercise 8. Sports  The yardage lines on a football field are parallel. Explain how the grounds crew could use Theorem 4–8 to know where to paint the yardage lines.  
(Example 3)

---

**Exercises**

**Practice**

Find \( x \) so that \( a \parallel b \).

9. \( a \parallel b \)

10. \( a \parallel b \)

11. \( a \parallel b \)

12. \( a \parallel b \)

13. \( a \parallel b \)

14. \( a \parallel b \)

---

Name the pairs of parallel lines or segments.

15. \( m \parallel n \)

16. \( AB \parallel CD \)

17. \( WS \parallel YZ \)

18. \( I \parallel J \)

19. \( m \parallel n \)

20. \( K \parallel L \)

21. Refer to the figure at the right.
   a. Find \( x \) so that \( AC \parallel DE \).
   b. Using the value that you found in part a, determine whether lines \( AB \) and \( CD \) are parallel.
22. **Solar Energy** The figure at the right shows how the sun’s rays reflect off special mirrors to provide electricity.

a. Are the rays from the sun, lines \( m \) and \( n \), parallel lines? Explain.

b. Are the reflected rays, lines \( p \) and \( q \), parallel lines? Explain.

23. **Construction** Carpenters use parallel wall studs in building supports for walls. Describe three ways a carpenter could guarantee that the wall studs \( AB \) and \( CD \) are parallel.

24. **Critical Thinking** In the Hands-On Geometry activity on page 162, you constructed a line through a point \( P \) parallel to a line \( \ell \). In 1795, Scottish mathematician John Playfair (1748–1819) provided the modern version of Euclid’s famous **Parallel Postulate**.

If there is a line and a point not on the line, then there exists exactly one line through the point that is parallel to the given line.

Explain the meaning of *exactly one* in the postulate. If you try to draw two lines parallel to a given line through a point not on the line, what happens?

25. Find the measure of each numbered angle.

26. Determine whether each statement is true or false. Explain your reasoning.

27. If \( LM = MJ \), then \( \overline{LM} \parallel \overline{MJ} \).

28. If \( XY \parallel YZ \), \( ST \parallel PQ \), and \( YZ \parallel PQ \), then \( \overline{XY} \parallel \overline{ST} \).

29. **Multiple Choice** The high temperature in Newport on January 12 was 6°C. The low temperature was -7°C. Find the range of the temperatures in Newport on this date.

A 1°C  B 6.5°C  C 7°C  D 13°C
The steepness of a line is called the 

**slope**. Slope is defined as the ratio of the **rise**, or vertical change, to the **run**, or horizontal change, as you move from one point on the line to another.

You can use two points on a line to find its slope. Consider the slope of \( AE \).

Notice that the slope of \( AE \) is always \( \frac{1}{2} \), regardless of the points chosen. The slope of a line is the same, or constant, everywhere along the line. This means that the choice of points used to find the slope of a line does not affect the slope. You can find the slope of a line as follows.

The slope of a vertical line, where \( x_1 \neq x_2 \), is undefined.

### Examples

#### Find the slope of each line.

1. \( m = \frac{2 - 4}{0 - (-5)} \) or \( -\frac{2}{5} \)
   
   The slope is \( -\frac{2}{5} \).

2. \( m = \frac{5 - 0}{4 - (-3)} \) or \( \frac{5}{7} \)
   
   The slope is \( \frac{5}{7} \).
the line through points at \((-4, 3)\) and \((2, 3)\)

\[ m = \frac{3 - 3}{2 - (-4)} = 0 \]

The slope is 0.

Your Turn

Find the slope of each line.

a. the line through points at \((-1, 3)\) and \((1, -3)\)

b. the line through points at \((3, 4)\) and \((3, -2)\)

\[ m = \frac{-2 - 4}{3 - 3} = -6 \]

The slope is undefined.

Examples 1–3 suggest that a line with a negative slope seems to be going downhill, a line with a positive slope seems to be going uphill, and a line with a zero slope is a horizontal line. As shown in Example 4, the slope of a vertical line is undefined.

<table>
<thead>
<tr>
<th>Slope Type</th>
<th>Graph</th>
</tr>
</thead>
<tbody>
<tr>
<td>Negative slope</td>
<td>( m &lt; 0 )</td>
</tr>
<tr>
<td>Positive slope</td>
<td>( m &gt; 0 )</td>
</tr>
<tr>
<td>0 slope</td>
<td>( m = 0 )</td>
</tr>
<tr>
<td>Undefined slope</td>
<td>( m ) is undefined</td>
</tr>
</tbody>
</table>

Materials:
- Grid paper
- Straightedge
- Protractor

Step 1

On a piece of grid paper, graph points \(A(-2, 0)\) and \(B(-3, -4)\). Using a straightedge, draw \(AB\).

Step 2

Graph points \(C(4, 4)\) and \(D(3, 0)\). Draw \(CD\). Using the definition of slope, find the slopes of \(AB\) and \(CD\).

Try These

1. Measure \(\angle BAD\) and \(\angle ADC\). What is true of these measures?
2. What special pair of angles do \(\angle BAD\) and \(\angle ADC\) form?
3. What is true of \(\overline{AB}\) and \(\overline{CD}\)?
This activity illustrates a special characteristic of parallel lines.

**Postulate 4–3** Two distinct nonvertical lines are parallel if and only if they have the same slope.

*All vertical lines are parallel.*

You can use a TI–92 calculator to study slopes of perpendicular lines.

**TI–92 Tutorial**
See pp. 758–761.

**Graphing Calculator Exploration**

**Step 1** First clear the screen by using 8:Clear All on the **F8** menu.

**Step 2** Press **F8**, select 9:Format . . . , and choose 2:RECTANGULAR under Coordinate Axes.

**Step 3** Draw a pair of nonvertical perpendicular lines on the coordinate plane.

**Step 4** Use 4:Slope on the **F6** menu to find the slope of each of the two perpendicular lines that you drew.

**Step 5** Use 6:Calculate on the **F6** menu to calculate the product of the slopes of the perpendicular lines.

**Try These**

1. What number did you obtain as the product of the slopes of the perpendicular lines?

2. Go to the point that you used to draw the first of your perpendicular lines. Drag this point to a different location. Describe what happens to the slopes of the perpendicular lines and to the product of the slopes.

3. Drag on one end of the first of your perpendicular lines. Describe what happens to the slopes and their product.

This activity illustrates a special characteristic of perpendicular lines.

**Postulate 4–4** Two nonvertical lines are perpendicular if and only if the product of their slopes is $-1$. 
A dragonfly has two sets of wings. Given $A(-2, -2), B(1, 2), C(-3, 6),$ and $D(5, 0)$, prove that the second set of wings is perpendicular to the body. In other words, show that $AB \perp CD$.

First, find the slopes of $AB$ and $CD$.

slope of $AB = \frac{2 - (-2)}{1 - (-2)} = \frac{4}{3}$

slope of $CD = \frac{0 - 6}{5 - (-3)} = \frac{-6}{8}$ or $-\frac{3}{4}$

The product of the slopes for $AB$ and $CD$ is $\frac{4}{3} \cdot -\frac{3}{4}$ or $-1$. So, $AB \perp CD$, and the second set of wings is perpendicular to the body.

c. Given $P(-2, 2), Q(2, 1), R(1, -1)$, and $S(5, -2)$, prove that $PQ \parallel RS$.

1. Describe a line whose slope is 0 and a line whose slope is undefined.

2. Estimate the slope of line $\ell$ shown at the right. Explain how you determined your estimate.

3. Sang Hee claims that a line with a slope of 2 is steeper than a line with a slope of $\frac{1}{4}$. Emily claims that a slope of $\frac{1}{4}$ is steeper than a slope of 2. Who is correct? Use a coordinate drawing to support your answer.

Guided Practice

Find the slope of each line. (Examples 1–4)

4. $\ell$ (slope $m$)

5. $\ell$ (slope $m$)

6. the line through points at $(-5, -2)$ and $(1, 2)$
Given each set of points, determine if $\overrightarrow{PQ}$ and $\overrightarrow{RS}$ are parallel, perpendicular, or neither.  \textbf{(Example 5)}

7. $P(9, 2), Q(2, 9), R(9, 5), S(0, 4)$
8. $P(6, 1), Q(4, 0), R(3, 5), S(7, 3)$

9. **Construction** Some building codes require the slope of a stairway to be no steeper than 0.88, or $\frac{22}{25}$. The stairs in Amad’s house measure 11 inches deep and 6 inches high. Do the stairs meet the code requirements? Explain. \textbf{(Example 5)}

Find the slope of each line.

10. $\text{the line through } (5, 6) \text{ and } (9, 0)$
11. $\text{the line through } (-2, 4) \text{ and } (0, -1)$
12. $\text{the line through } (-4, 9) \text{ and } (3, 0)$
13. $\text{the line through } (2, 5) \text{ and } (0, -2)$
14. $\text{the line through } (-3, 8) \text{ and } (-3, 2)$
15. $\text{the line through } (-3, 5) \text{ and } (4, -4)$

16. the line through $(\frac{1}{2}, 5)$ and $(2\frac{1}{2}, 1)$
17. the line through $(1, 3.5)$ and $(6, 3.5)$
18. the line through $(-1, -7)$ and $(3, -1)$

Given each set of points, determine if $\overrightarrow{JK}$ and $\overrightarrow{LM}$ are parallel, perpendicular, or neither.

19. $J(-4, 11), K(-6, 3), L(7, 7), M(6, 3)$
20. $J(6, 9), K(4, 6), L(0, 8), M(3, 6)$
21. $J(-8, 1), K(-5, -8), L(0, 10), M(3, 11)$
22. $J(6, 3), K(-7, 3), L(-4, -5), M(1, -5)$
23. $J(-1, 5), K(2, -3), L(7, 9), M(2, 6)$
24. $J(3, -2), K(5, -9), L(6, 4), M(4, -3)$

25. Find the slope of the line passing through points at $(-7, 4)$ and $(2, 9)$.

26. $C(r, -5)$ and $D(5, 3)$ are two points on a line. If the slope of the line is $\frac{2}{3}$, find the value of $r$.  \textbf{(Example 5)}
Applications and Problem Solving

27. **Sports** Refer to the application at the beginning of the lesson. Find the *run* of a hill with a 36-foot *rise* if the hill has a slope of 0.02.

28. **Construction** To be efficient, gutters should drop $\frac{1}{4}$ inch for every 4 feet that they run toward a downspout. What is the desired slope of a gutter?

29. **Critical Thinking** Use slope to determine if $A(2, 4), B(5, 8), C(13, 2),$ and $D(10, -2)$ are the vertices of a rectangle. Explain.

Mixed Review

30. Name the pairs of parallel segments. *(Lesson 4–4)*

31. Find the measure of each numbered angle. *(Lesson 4–3)*

In the figure, $\overline{XA}$ and $\overline{XD}$ are opposite rays. *(Lesson 3–4)*

32. Which angle forms a linear pair with $\angle AXB$?

33. Name all pairs of adjacent angles.

34. **Multiple Choice** What is the hypothesis in the following statement? *(Lesson 1–4)*

   Angles are congruent if they have the same measure.

   A congruent     B they have the same measure
   C angles are congruent D not congruent

Quiz 2

Lessons 4–4 and 4–5

Find $x$ so that $a \parallel b$. *(Lesson 4–4)*

4. **Music** On the panpipe at the right, find the slope of $\overline{GH}$. *(Lesson 4–5)*

5. Given $P(-6, 1), Q(6, 4), R(3, 4),$ and $S(2, 8)$, determine if $PQ$ and $RS$ are parallel, perpendicular, or neither. *(Lesson 4–5)*
The equation \( y = 2x - 1 \) is called a **linear equation** because its graph is a straight line. We can substitute different values for \( x \) in the equation to find corresponding values for \( y \), as shown in the table at the right.

<table>
<thead>
<tr>
<th>( x )</th>
<th>( 2x - 1 )</th>
<th>( y )</th>
<th>( (x, y) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>2(0) - 1</td>
<td>-1</td>
<td>(0, -1)</td>
</tr>
<tr>
<td>1</td>
<td>2(1) - 1</td>
<td>1</td>
<td>(1, 1)</td>
</tr>
<tr>
<td>2</td>
<td>2(2) - 1</td>
<td>3</td>
<td>(2, 3)</td>
</tr>
<tr>
<td>3</td>
<td>2(3) - 1</td>
<td>5</td>
<td>(3, 5)</td>
</tr>
</tbody>
</table>

We can then graph the ordered pairs \((x, y)\). Notice that there is one line that contains all four points. There are many more points whose ordered pairs are solutions of \( y = 2x - 1 \). These points also lie on the line.

To find the slope of this line, choose any two points on the line, such as \( B(1, 1) \) and \( C(2, 3) \).

\[
m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{Definition of slope}
\]

\[
= \frac{3 - 1}{2 - 1} \quad \text{Replace } y_2 \text{ with } 3, \text{ and } y_1 \text{ with } 1.
\]

\[
= \frac{2}{1} \quad \text{Replace } x_2 \text{ with } 2, \text{ and } x_1 \text{ with } 1.
\]

\[
= 2 \quad \text{or } 2
\]

Now look at the graph of \( y = 2x - 1 \). The \( y \)-value of the point where the line crosses the \( y \)-axis is \(-1\). This value is called the **\( y \)-intercept** of the line.

\[
y = 2x - 1
\]

**slope** \( \uparrow \) **\( y \)-intercept**

Most linear equations can be written in the form \( y = mx + b \). This form is called the **slope-intercept form**.

**Slope-Intercept Form**

An equation of the line having slope \( m \) and \( y \)-intercept \( b \) is

\[
y = mx + b
\]

**What You’ll Learn**

You’ll learn to write and graph equations of lines.

**Why It’s Important**

Communication

Telephone company representatives can use linear equations to determine the cost of telephone calls. See Exercise 35.
Name the slope and \( y \)-intercept of the graph of each equation.

1. \( y = \frac{1}{2}x + 5 \)
   - The slope is \( \frac{1}{2} \).
   - The \( y \)-intercept is 5.

2. \( y = 3 \)
   - The slope is 0.
   - The \( y \)-intercept is 3.

3. \( x = -2 \)
   - The slope is undefined.
   - There is no \( y \)-intercept.

4. \( 2x - 3y = 18 \)
   - Rewrite the equation in slope-intercept form by solving for \( y \).
     
     \[
     2x - 3y = 18
     \]
     
     Subtract 2x from each side.
     
     \[
     2x - 3y - 2x = 18 - 2x
     \]
     
     \[
     -3y = 18 - 2x
     \]
     
     Divide each side by -3.
     
     \[
     \frac{-3y}{-3} = \frac{18 - 2x}{-3}
     \]
     
     \[
     y = -6 + \frac{2}{3}x
     \]
     
     Simplify.
     
     \[
     y = \frac{2}{3}x - 6
     \]
     
     Write in slope-intercept form.
     
     The slope is \( \frac{2}{3} \). The \( y \)-intercept is -6.

Your Turn

a. \( y = -x + 8 \)

b. \( x + 4y = 24 \)

c. \( y = -1 \)

d. \( x = 10 \)

e. Graph \( -x + 3y = 9 \) using the slope and \( y \)-intercept.

Graph \( 2x + y = 3 \) using the slope and \( y \)-intercept.

First, rewrite the equation in slope-intercept form.

\[
2x + y = 3
\]

Subtract 2x from each side.

\[
2x + y - 2x = 3 - 2x
\]

\[
y = 3 - 2x
\]

Write in slope-intercept form.

The \( y \)-intercept is 3. So, the point at (0, 3) must be on the line. Since the slope is \( -\frac{2}{1} \), plot a point by using a rise of -2 units (down) and a run of 1 unit (right). Draw a line through the points.

Your Turn

Graph \( -x + 3y = 9 \) using the slope and \( y \)-intercept.
The graphs of lines \( \ell \), \( m \), and \( t \) are shown at the right.

\[
\ell: \quad y = 2x - 3
\]
\[
m: \quad y = 2x + 6
\]
\[
t: \quad y = -\frac{1}{2}x + 3
\]

Notice that \( \ell \) appears to be parallel to \( m \). You can verify this by Postulate 4–3, since the slopes of \( \ell \) and \( m \) are the same. Also, \( t \) appears to be perpendicular to \( \ell \) and \( m \). You can verify this by Postulate 4–4, since the product of the slope of \( t \) and the slope of \( \ell \) or \( m \) is \(-1\). Thus, the slope-intercept form can be used to write the equation of another line.

**Example 6**

Write an equation of the line parallel to the graph of \( y = 2x - 5 \) that passes through the point at \((3, 7)\).

**Explore**  The equation of the line will be in the form \( y = mx + b \). You need to find the slope \( m \) and the \( y \)-intercept \( b \).

**Plan**  Because the lines are parallel, they must have the same slope. The slope of the given line is 2, so the slope \( m \) of the line parallel to the graph of \( y = 2x - 5 \) must be 2.

To find \( b \), use the ordered pair \((3, 7)\) and substitute for \( m \), \( x \), and \( y \) in the slope-intercept form.

**Solve**  
\[
y = mx + b
\]
\[
7 = 2(3) + b \quad \text{Replace } m \text{ with } 2 \text{ and } (x, y) \text{ with } (3, 7).
\]
\[
7 = 6 + b
\]
\[
7 - 6 = 6 + b - 6 \quad \text{Subtract } 6 \text{ from each side.}
\]
\[
1 = b
\]

The value of \( b \) is 1. So, the equation of the line is \( y = 2x + 1 \).

**Examine**  The graphs of \( y = 2x - 5 \) and \( y = 2x + 1 \) both have the same slope, 2, so the lines are parallel. Since \( 7 = 2(3) + 1 \), the graph of \( y = 2x + 1 \) passes through the point at \((3, 7)\). The solution satisfies the conditions given.

**Your Turn**

Write each equation in slope-intercept form.

**f.**  Write an equation of the line parallel to the graph of \( 3x + y = 6 \) that passes through the point at \((1, 4)\).

**g.**  Write an equation of the line perpendicular to the graph of \( y = \frac{1}{4}x + 5 \) that passes through the point at \((-3, 8)\).
Check for Understanding

Communicating Mathematics

1. Explain why \( y = mx + b \) is called the slope-intercept form of the equation of a line.

2. Explain how you know that lines \( \ell, m, \) and \( n \) are parallel. Then name the \( y \)-intercept for each line.

Guided Practice

+ Getting Ready + Solve each equation for \( y \).

<table>
<thead>
<tr>
<th>Sample: ( 8x + 4y = 1 )</th>
<th>Solution: ( 4y = 1 - 8x ) or ( y = \frac{1}{4} - 2x )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( 3. y - 6x = -3 )</td>
<td>( 4. x + 7y = 14 )</td>
</tr>
</tbody>
</table>

Name the slope and \( y \)-intercept of the graph of each equation.
(Examples 1–4)

| \( 6. y = 2x + 6 \) | \( 7. 3x + 2y = 8 \) |

Graph each equation using the slope and \( y \)-intercept.
(Example 5)

| \( 8. y = -x + 4 \) | \( 9. 2x - 5y = 10 \) |

Write an equation of the line satisfying the given conditions.
(Example 6)

| \( 10. \) slope = 4, goes through the point at \((-1, 3)\) | \( 11. \) parallel to the graph of \( y = -2x + 6 \), passes through the point at \((-4, 4)\) |

12. Nutrition In the equation \( C = 15f + 68 \), \( C \) represents the number of Calories in a strawberry breakfast bar, and \( f \) represents the number of fat grams.
(Example 1)

a. What is the slope of the line? What does it represent?

b. What is the \( y \)-intercept? What does it represent?
Practice

Name the slope and \( y \)-intercept of the graph of each equation.

13. \( y = 9x + 1 \)
14. \( 7x + y = 12 \)
15. \( 3x - 2y = 18 \)
16. \( x = 6 \)
17. \( y = 5 \)
18. \( 3x + 4y = 2 \)

Graph each equation using the slope and \( y \)-intercept.

19. \( y = 3x - 5 \)
20. \( y = -x + 6 \)
21. \( y + 7x = 4 \)
22. \( \frac{1}{2}x + 2y = 9 \)
23. \( \frac{1}{3}x - y = 2 \)
24. \( 4x - 3y = -6 \)

Write an equation of the line satisfying the given conditions.

25. slope = 3, goes through the point at \((-1, 4)\)
26. parallel to the graph of \( y = -2x - 6 \), passes through the point at \((4, 4)\)
27. parallel to the graph of \( 4x + y = 9 \), passes through the point at \((0, -5)\)
28. parallel to the \( x \)-axis, passes through the point at \((-3, -6)\)
29. slope is undefined, passes through the point at \((-3, 7)\)
30. perpendicular to the graph of \( y = \frac{1}{2}x - 3 \), passes through the point at \((5, -4)\)

Choose the correct graph of lines \( a, b, c, \) or \( d \) for each equation.

31. \( y = 2x + 1 \)
32. \( y = 2x + 3 \)
33. \( y = -2x - 1 \)
34. \( y = -2x + 3 \)

35. Communication One telephone company’s charges are given by the equation \( y = 0.40x + 0.99 \), where \( y \) represents the total cost in dollars for a telephone call and \( x \) represents the length of the call in minutes.
   a. Make a table of values showing what a telephone call will cost after 0, 1, 2, 3, 4, and 5 minutes.
   b. Graph the values in your table.
   c. What is the slope of the line? What does it represent?
   d. What is the \( y \)-intercept of the line? What does it represent?
36. **Sports** The graph at the right shows the distance a baseball can be hit when it is pitched at different speeds.
   a. What is the \(y\)-intercept? What does this value represent?
   b. Estimate the slope.
   c. Write an equation of the line.

37. **Critical Thinking** Explain how you could find an equation of a line if you are only given the coordinates of two points on the line.

### Mixed Review

The graph at the right shows the estimated cost of wireless phone use from 1998 to 2003.  
(Lesson 4–5)

38. Which section of the graph shows when the greatest change occurred? How does its slope compare to the rest of the graph?

39. Describe the slope of a graph showing an increase in cost.

40. Find \(x\) so that \(a \parallel b\).  
   (Lesson 4–4)

41. Haloke used the design shown below in a quilt she made for her grandmother. Name all the angles with \(Q\) as a vertex.  
   (Lesson 3–1)

42. **Algebra** What is the length of a rectangle with area 108 square inches and width 8 inches?  
   (Lesson 1–6)

43. **Extended Response** Just by looking, which segment appears to be longer, \(AJ\) or \(KR\)? Use a ruler to measure the two segments. What do you discover?  
   (Lesson 1–5)

44. **Multiple Choice** Which is not a plane represented in the figure?  
   (Lesson 1–3)
   
   A  \(ABD\)  
   B  \(CDF\)  
   C  \(BFE\)  
   D  \(ADF\)

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Understanding and Using the Vocabulary

After completing this chapter, you should be able to define each term, property, or phrase and give an example or two of each.

**Geometry**
- alternate exterior angles (p. 148)
- alternate interior angles (p. 148)
- consecutive interior angles (p. 148)
- corresponding angles (p. 156)
- exterior angles (p. 148)
- finite (p. 154)
- great circle (p. 154)
- interior angles (p. 148)
- line (p. 154)
- line of latitude (p. 154)
- line of longitude (p. 154)
- parallel lines (p. 142)
- parallel planes (p. 142)
- skew lines (p. 143)
- transversal (p. 148)

**Algebra**
- linear equation (p. 174)
- slope (p. 168)
- slope-intercept form (p. 174)
- y-intercept (p. 174)

Choose the letter of the term that best describes each set of angles or lines.

1. $\angle 2$ and $\angle 7$
2. $\angle 1$, $\angle 3$, $\angle 6$, $\angle 8$
3. $\angle 5$ and $\angle 1$
4. lines $m$ and $n$
5. $\angle 7$ and $\angle 4$
6. line $q$
7. $\angle 2$, $\angle 4$, $\angle 5$, $\angle 7$
8. $\angle 1$ and $\angle 6$
9. lines $q$ and $p$
10. lines $p$ and $m$

Skills and Concepts

**Objectives and Examples**

- **Lesson 4–1** Describe relationships among lines, parts of lines, and planes.

  In the prism, plane $QRS$ is parallel to plane $TUV$.

  $\overline{TW}$ and $\overline{UV}$ are parallel to $\overline{RS}$.

  $\overline{QR}$, $\overline{TU}$, $\overline{RS}$, $\overline{UV}$ intersect $\overline{RU}$.

  $\overline{RS}$, $\overline{SP}$, $\overline{UV}$, and $\overline{WV}$ are skew to $\overline{QT}$.

**Review Exercises**

Describe each pair of segments in the prism as **parallel**, **skew**, or **intersecting**.

11. $\overline{HB}$, $\overline{FD}$
12. $\overline{BC}$, $\overline{AG}$
13. $\overline{EC}$, $\overline{HE}$

Name the parts of the prism.

14. six planes
15. all segments skew to $\overline{GE}$
16. all segments parallel to $\overline{GF}$
**Objectives and Examples**

- **Lesson 4–2** Identify the relationships among pairs of interior and exterior angles formed by two parallel lines and a transversal.

  \[ \angle 3 \text{ and } \angle 8 \text{ are alternate interior angles, so they are congruent.} \]

  \[ \angle 1 \text{ and } \angle 8 \text{ are consecutive interior angles, so they are supplementary.} \]

  \[ \angle 4 \text{ and } \angle 7 \text{ are alternate exterior angles, so they are congruent.} \]

- **Lesson 4–3** Identify the relationships among pairs of corresponding angles formed by two parallel lines and a transversal.

  If \( s \parallel t \), which angles are congruent to \( \angle 2 \)?

  \[ \angle 2 \equiv \angle 5 \quad \text{Vertical angles are congruent.} \]

  \[ \angle 2 \equiv \angle 3 \quad \text{Postulate 4–1} \]

  \[ \angle 3 \equiv \angle 7 \quad \text{Vertical angles are congruent.} \]

  Therefore, \( \angle 5 \), \( \angle 3 \), and \( \angle 7 \) are congruent to \( \angle 2 \).

- **Lesson 4–4** Identify conditions that produce parallel lines and construct parallel lines.

  Find \( x \) so that \( JK \parallel MN \).

  \[ \angle JLM \text{ and } \angle LMN \text{ are alternate interior angles. If } \angle JLM \equiv \angle LMN, \text{ then } JK \parallel MN. \]

  \[ m\angle JLM = m\angle LMN \]

  \[ 63 = 5x - 2 \quad \text{Substitution} \]

  \[ 65 = 5x \quad \text{Add 2 to each side.} \]

  \[ 13 = x \quad \text{Divide each side by 5.} \]

**Review Exercises**

**Review Exercises**

- Identify each pair of angles as alternate interior, alternate exterior, consecutive interior, or vertical.

  17. \( \angle 1 \text{ and } \angle 6 \)

  18. \( \angle 4 \text{ and } \angle 2 \)

  19. \( \angle 3 \text{ and } \angle 8 \)

  20. \( \angle 7 \text{ and } \angle 3 \)

  **Exercises 17–24**

- If \( m\angle 1 = 124 \), find the measure of each angle. Give a reason for each answer.

  21. \( \angle 3 \)

  22. \( \angle 4 \)

  23. \( \angle 6 \)

  24. \( \angle 8 \)

- Name all angles congruent to the given angle. Give a reason for each answer.

  25. \( \angle 2 \)

  26. \( \angle 5 \)

  27. \( \angle 10 \)

- Find the measure of each numbered angle.

  28. \[ \begin{array}{ccc} 4 & 5 & 6 \\ 3 & 33 & 7 \\ 2 & 8 & 10 \end{array} \]

  29. \[ \begin{array}{ccc} 11 & 129 \end{array} \]

  30. \( \text{Find } x \text{ so that } c \parallel d. \)

  31. \[ \begin{array}{ccc} 107 & \text{c} & \text{d} \\ 2x - 9 & \text{d} \end{array} \]

- Name the pairs of parallel lines or segments.

  32. \[ \begin{array}{ccc} B & V & R \\ 87 & 93 & 8 \end{array} \]

  33. \[ \begin{array}{ccc} S & T & R \\ 42 & 39 & 39 \end{array} \]
Chapter 4 Study Guide and Assessment

Objectives and Examples

- **Lesson 4–5** Find the slopes of lines and use slope to identify parallel and perpendicular lines.

  Given \( A(9, 2), D(6, 3), F(-5, 7), \) and \( S(-4, 10) \), is \( AD \perp FS \), \( AD \parallel FS \), or neither?

  \[
  \text{slope of } AD = \frac{3 - 2}{6 - 9} = \frac{-1}{3} \\
  \text{slope of } FS = \frac{10 - 7}{-4 - (-5)} = \frac{3}{1} \text{ or } 3 \\
  \]

  Since \( \left(-\frac{1}{3}\right) \left(\frac{3}{1}\right) = -1 \), \( AD \perp FS \).

- **Lesson 4–6** Write and graph equations of lines.

  **Slope-intercept form:**
  \[
  y = mx + b \\
  \text{slope } \uparrow \uparrow \uparrow \text{ y-intercept}
  \]

  To graph a linear equation using slope and y-intercept, rewrite the equation by solving for \( y \).

Review Exercises

Find the slope of each line.

34. \( a \)
35. \( b \)
36. \( c \)

Given each set of points, determine if \( GH \) and \( PQ \) are parallel, perpendicular, or neither.

37. \( G(-4, 3), H(10, -9), P(8, 6), Q(1, 0) \)
38. \( G(11, 0), H(3, -7), P(4, 16), Q(-4, 9) \)

Name the slope and y-intercept of the graph of each equation. Then graph the equation.

39. \( y = -\frac{3}{5}x + 1 \)
40. \( 2x + 5y = 20 \)

41. Write an equation of the line perpendicular to the graph of \( y = -2x + 4 \) that passes through the point at \((-8, 3)\).

Applications and Problem Solving

42. **Gymnastics** Describe bars \( \ell \) and \( m \) on the equipment below as parallel, skew, or intersecting. (Lesson 4–1)

43. **Construction** A flight of stairs is parallel to the overhead ceiling. If \( x = 122 \), find \( y \). (Lesson 4–4)
Choose the letter on the right that identifies each angle pair.

1. \( \angle 5 \) and \( \angle 16 \)  
   a. corresponding angles

2. \( \angle 9 \) and \( \angle 3 \)  
   b. consecutive interior angles

3. \( \angle 10 \) and \( \angle 13 \)  
   c. alternate interior angles

4. \( \angle 11 \) and \( \angle 9 \)  
   d. alternate exterior angles

5. \( \angle 2 \) and \( \angle 7 \)  
   e. vertical angles

Describe each pair of segments or planes in the prism as parallel, skew, or intersecting.

6. \( \overline{IJ} \) and \( \overline{EF} \)

7. plane \( JBI \) and plane \( IGH \)

8. \( \overline{CG} \) and \( \overline{AB} \)

9. plane \( ADF \) and plane \( HBC \)

10. Name all segments parallel to \( \overline{AD} \).

11. Name all segments that intersect \( \overline{BH} \).

In the figure, \( q \parallel r \).

12. If \( m\angle 7 = 88 \), find the measure of each numbered angle.

13. If \( \angle 1 \) is a right angle, name two pairs of perpendicular lines.

14. If \( m\angle 5 = 5x \) and \( m\angle 7 = 2x + 63 \), find \( m\angle 5 \).

Name the parallel segments formed if the following angles are congruent.

15. \( \angle 2 \) and \( \angle 6 \)

16. \( \angle 3 \) and \( \angle 4 \)

17. If \( m\angle DCB = 12x - 3 \) and \( m\angle 7 = 8x + 3 \), find \( x \) so that \( AD \parallel BC \).

Given each set of points, find the slopes of \( MN \) and \( UV \). Then determine whether the two lines are parallel, perpendicular, or neither.

18. \( M(-3, -5), N(-3, 4), U(7, -2), V(4, -5) \)

19. \( M(2, 12), N(-8, 9), U(8, 4), V(-2, 1) \)

20. \( M(4, 8), N(9, 2), U(0, 3), V(-6, -2) \)

21. Graph the equation \( 3x + y = 1 \) using the slope and y-intercept.

22. Find and graph the equation of the line with slope \(-1\) passing through the point at \((2, 3)\).

23. Find the equation of the line parallel to the \( y \)-axis and passing through the point at \((-4, 7)\).

24. **Meteorology** The weather symbol at the right represents a heavy thunderstorm. If \( AB \) and \( CD \) are parallel segments and \( m\angle B = 85\), find \( m\angle C \).

25. **Civil Engineering** A public parking lot is constructed so that all parking stalls in an aisle are parallel. If \( m\angle KLA = 43\), find \( m\angle PKR \).

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Data Analysis Problems

Proficiency tests usually include several problems on interpreting graphs and creating graphs from data. The SAT and ACT may include a few questions on interpreting graphs. Often a graph is used to answer two or more questions.

You’ll need to understand these ways of representing data: bar graphs, circle graphs, line graphs, stem-and-leaf plots, histograms, and frequency tables.

State Test Example

The table below shows the number of employees who earn certain hourly wages at two different companies.

<table>
<thead>
<tr>
<th>Hourly Wage ($)</th>
<th>Number of Employees</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Company 1</td>
</tr>
<tr>
<td>6.00</td>
<td>3</td>
</tr>
<tr>
<td>6.50</td>
<td>5</td>
</tr>
<tr>
<td>7.00</td>
<td>6</td>
</tr>
<tr>
<td>7.50</td>
<td>4</td>
</tr>
<tr>
<td>8.00</td>
<td>1</td>
</tr>
</tbody>
</table>

Construct a double-bar graph to show the number of employees at each company who earn the given hourly wages.

Hint Decide what quantities will be shown on each axis of your graph. Label the axes.

Solution Draw the double-bar graph. Put the wages on the horizontal axis and the number of employees on the vertical axis.

SAT Example

For what percent of the time was Sara driving 40 miles per hour or faster?

A 20%  B 25%  C 33\%  D 40%  E 50%

Hint Don’t mix units, like hours and minutes. In this case, use hours.

Solution The total time Sara drove is 3 hours (from 1:00 until 4:00). She drove 40 miles per hour or faster from 2:30 to 4:00, or \(\frac{1}{2}\) hours.

The fraction of the time she drove 40 mph or faster is \(\frac{\frac{1}{2}}{3}\) or \(\frac{1}{2}\). The equivalent percent is 50%.

So, the answer is E.
Chapter 4 Preparing for Standardized Tests

After you work each problem, record your answer on the answer sheet provided or on a sheet of paper.

**Multiple Choice**

1. What is a reasonable conclusion from the information given?

**Ticket Sales at Bob’s Ticket Outlet**

- Rock Concerts: 24%
- Classical Concerts: 18%
- Country Music Concerts: 28%
- Plays: 12%
- Other: 18%

A Fewer than 20 customers purchased classical concert tickets last month.
B Plays are more popular than country music concerts at Bob’s.
C Rock concerts are less popular than country music concerts at Bob’s.
D Bob doesn’t sell rap concert tickets.

2. \((-2)^3 + (3)^{-2} + \frac{8}{9}\) =

A -7  
B -1\frac{7}{9}  
C \frac{8}{9}  
D 1\frac{7}{9}  
E 12

3. Kendra has a collection of 80 tapes. If 40% are jazz tapes and the rest are blues tapes, how many blues tapes does she have?

A 32  
B 40  
C 42  
D 48  
E 50

4. Cody has 3 pairs of jeans and 4 sweatshirts. How many combinations of 1 pair of jeans and 1 sweatshirt can he wear?

A 3  
B 4  
C 7  
D 12

5. If \(3x + 7 = 28\), what is \(x\)?

A 4  
B 5  
C 6  
D 7  
E 8

6. \(FB\) and \(EC\) are parallel, and the measure of \(\angle CXD\) is 62. Find the measure of \(\angle FYX\).

A 28  
B 62  
C 90  
D 118

7. In a stem-and-leaf plot of the data in the chart, which numbers would be the best choice for the stems?

**Average Temperature (°F)**

<table>
<thead>
<tr>
<th></th>
<th>52</th>
<th>55</th>
<th>49</th>
<th>51</th>
<th>57</th>
<th>66</th>
</tr>
</thead>
<tbody>
<tr>
<td>62</td>
<td>61</td>
<td>61</td>
<td>73</td>
<td>78</td>
<td>76</td>
<td></td>
</tr>
<tr>
<td>69</td>
<td>58</td>
<td>59</td>
<td>74</td>
<td>78</td>
<td>79</td>
<td></td>
</tr>
</tbody>
</table>

A 5–7  
B 4–7  
C 0–7  
D 0–9

8. What is the \(y\)-intercept of line \(MN\)?

A -4  
B 2  
C -2  
D 0

9. Six cards are numbered 0 through 5. Two are selected without replacement. What is the probability that their sum is 4?

**Extended Response**

10. The numbers of visitors each day to the local history museum during the month of June are shown below.

| 184–185 C4STP-845773 3/20/03 8:42 AM Page 185 mac62 mac62:1st_TC: |

| 11 19 8 7 18 43 22 18 14 21 19 |
| 41 61 36 16 16 14 24 31 64 29 24 |
| 27 33 31 71 89 61 41 34 |

Part A Construct a frequency table for the data.

Part B Construct a histogram that represents the data.

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